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E-Bayesian estimation for the Burr type XII model based on type-2 censoring

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ABSTRACT

This paper is concerned with using the E-Bayesian method [M. Han, Applied Mathematical Modeling (2009) 1915–1922] for computing estimates for the parameter and reliability function of the Burr type XII distribution based on type-2 censored samples. The estimates are obtained based on squared error and LINEX loss functions. A comparison between the new method and the corresponding Bayes and maximum likelihood techniques is made using the Monte Carlo simulation.

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1. Introduction

The two-parameter Burr type XII (Burr(α, β)) distribution with probability density function (*pdf*)

$$f(\mathbf{x}) = \alpha \beta \mathbf{x}^{\alpha - 1} (1 + \mathbf{x}^{\alpha})^{-(\beta + 1)}, \qquad \mathbf{x} > \mathbf{0}, \quad (\alpha > \mathbf{0}, \ \beta > \mathbf{0}),$$
(1.1)

and the reliability function

$$R(t) = (1 + t^{\alpha})^{-\beta}, \qquad t > 0,$$
(1.2)

was first introduced in literature by Burr [1]. The Burr(α, β) distribution has been proposed as a lifetime model by Rodriguez [2] and Tadikamalla [3]. Lewis [4] proposed the use of the Burr(α, β) distribution as a model in accelerated life test data representing times to breakdown of an insulating fluid. Inferences and predictions for the Burr(α, β) distribution and some of its testing measures based on complete and censored samples were discussed by many authors. Evans and Ragab [5] obtained Bayes estimates of β and the reliability function based on type-2 censored samples. AL-Hussaini and Jaheen [6,7] obtained Bayesian estimation for the two parameters, reliability and failure rate functions of the Burr XII distribution. Ali Mousa [8] obtained empirical Bayes estimation of the parameter β and the reliability function based on accelerated type-2 censored data. Based on complete samples, Moore and Papadopoulos [9] obtained Bayes estimates of β and the reliability function when the parameter α is assumed to be known. Ali Mousa and Jaheen [10] obtained Bayes approximate estimates for the two parameters and reliability function of the Burr(α, β) distribution based on progressive type-2 censored samples. Jaheen [11] used the generalized order statistics for obtaining Bayesian inference for the Burr XII model. Based on progressive samples from the Burr(α, β) distribution, Soliman [12] obtained the Bayes estimates using both the symmetric (squared error) loss function, and asymmetric (LINEX, General Entropy) loss functions.

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